Equal Clustering Makes Min-Max Modular Support Vector Machine More Efficient

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Equal Clustering Makes Min-Max Modular Support Vector Machine More Efficient

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Abstract—Support vector machines has training time at least quadratic in the number of examples, so it is hopeless to use it to solve large-scale problems. In this paper, a novel clustering algorithm that can equally partition training data sets is proposed to improve the performance of the min-max modular support vector machine (M3-SVM). The simulation results indicate that the proposed clustering method can not only promote the generalization accuracy of the M3-SVM, but also speed up training and reduce the number of support vectors in comparison with the existing random task decomposition method.

I. INTRODUCTION

Today there are many very large-scale data sets like public-health data, gene expression data, national economics data, and geographic information data. By using these very large data sets, researchers can get higher generalization accuracy, discover infrequent special cases, and avoid over-fitting. However, most of existing machine learning methods such as support vector machine are hard to be used to deal with these very large data sets because both their learning time and space complexity have at least quadratic in the number of examples. Therefore, one of the most challenging problems in machine learning community is to develop new learning model to efficiently handle these large data sets. Many efforts are made to scale SVMs, such as using clustering methods to preprocess large training data [1] [2], using cascade and parallel methods to filter non-support vectors [3] [4] [5].

According to Provost [6], parallelism is a good strategy for dealing with large-scale data sets. In the training phase of parallel learning methods, a large training data set is first decomposed and parallelly processed, then many local learners are obtained. In recognition phase, an unknown sample is presented to all the learners, the outputs of all the learners are integrated to make a final solution to the original problem [7] [8]. Obviously, the performance of parallel method heavily depends on the integration principle of learners and the decomposition strategy of training data set. In our previous work, a modular support vector machine, called min-max modular support vector machine (M3-SVM) [9], was proposed to overcome the drawback of traditional SVMs. With two module combination principles, namely the minimization principle and the maximization principle, and a random task partition strategy, M3-SVM has been successfully applied to various fields such as text classification [9], face recognition [10], and gender recognition [11].

However, how to choose a task decomposition strategy according to integration principle to make parallel learning method work efficiently? In essence, the integration principle of M3-SVM is to dynamically choose a appropriate local learner to classify an input sample. From this point of view, training data should be partitioned according to its distribution in feature space. This law is extremely needed when all samples in training data set are not identically distributed. Random data partition ignores this law and works not very well [12]. In this paper, a novel clustering method is proposed to decompose large training data set into many smaller subsets, which are roughly the same in size. All the experiments show that the proposed clustering method can not only promote the M3-SVM’s generalization accuracy, but also speed up training and reduce the number of support vectors (SVs) in comparison with the traditional random task decomposition method.

II. MIN-MAX MODULAR SUPPORT VECTOR MACHINE

Min-max modular (M3) neural network [8] is a realization of the principle “divide-and-conquer” in machine learning. By M3-neural network, a large-scale problem is divided into many smaller and simpler subproblems. In essence, M3-neural network is a general framework for machine learning. M3-neural network can easily address multiclass problems. Here for simplicity of discussion, only two-class classification problems are considered. Given positive training data set \( \mathcal{X}^+ = \{(X_i^+, +1)\}_{i=1}^{N^+} \) and negative training data set \( \mathcal{X}^- = \{(X_i^-, -1)\}_{i=1}^{N^-} \), where \( X_i^+ \in \mathcal{R}^n \) and \( X_i^- \in \mathcal{R}^n \) denote the ith positive and negative training sample respectively, and \( N^+ \) and \( N^- \) denote the number of positive and negative training samples, respectively. The entire training data set can be defined as \( S = \mathcal{X}^+ \cup \mathcal{X}^- \).

In training phase, min-max modular method decomposes \( \mathcal{X}^+ \) and \( \mathcal{X}^- \) into \( K^+ \) and \( K^- \) roughly equal subsets respectively by using a data partition strategy.

\[
\mathcal{X}^+ = \bigcup_{i=1}^{K^+} \mathcal{X}_i^+, \quad \mathcal{X}_i^+ = \{(X_{m_i}^+, +1)\}_{m=1}^{N_i^+}, \quad i = 1, 2, ..., K^+
\]

\[
\mathcal{X}^- = \bigcup_{j=1}^{K^-} \mathcal{X}_j^-, \quad \mathcal{X}_j^- = \{(X_{n_j}^-, -1)\}_{n=1}^{N_j^-}, \quad j = 1, 2, ..., K^-
\]

(1)
The data decomposition problem can be described as follows: given a data set $X \in \mathbb{R}^n$, $m$ subsets $C_i \in \mathbb{R}^n$ ($i = 1, 2, ..., m$) are found to satisfy $\bigcup_{i=1}^m C_i = X$ and $\bigcap_{i=1}^m C_i = \emptyset$. When training data are not identically distributed, the effectiveness of random data partition method will be unstable and sometimes becomes very bad [12]. In order to handle these problems, one needs to generate spatially localized clusters that contain (nearly) equal number of samples to keep load balance. Based on the algorithm “GeoClust” [13], a modified clustering method is proposed in this paper. In our proposed method, the way to generate balanced spatially localized clusters needs to solve the unconstrained nonlinear programming problem as follows:

$$\text{Minimize : } h = \max_{i=1}^m |W_i - \bar{W}|$$

where $c_i$ and $W_i$ denote the center vector and number of samples in the $i$th cluster, respectively, and $m$ denotes the number of partition. $\bar{W}$ is the number of samples per cluster, i.e., $\bar{W} = \left\lfloor \frac{N}{m} \right\rfloor$. The objective function $h$ evaluates the degree of balance among all clusters, the smaller the value of $h$, the more balanced all clusters get. The algorithm is shown in Fig. 2.

In our proposed equal clustering method, if two cluster contain different number of samples, the center $c_i$ of smaller cluster $C_i$ will move toward to the center $c_j$ of larger cluster $C_j$ while $c_j$ will move toward along the direction of the vector $c_j - c_i$. Two parameters $\alpha$ and $\varepsilon$ control the movement degree of the centers. In the paper, we set $\text{maxiter} = 6000$, $\alpha = 0.01 \times 10^{-\frac{1}{14} \left\lfloor \frac{1}{m^2} \right\rfloor}$, $l = 3$, and $\varepsilon = \left\lfloor \frac{N}{m^2} \right\rfloor$. Apparently, the time complexity of this cluster method is less or equal than $O(m \times \text{maxiter})$ and there is no memory thrashing in our method even though data set is very large.

Comparing to the algorithm GeoClust, there are two modifications made to improve it. The first is that, a program break-up condition, “If $h < \varepsilon$, then break” is added into the algorithm. This modification can ensure that the algorithm stops at once if the prescribed balance condition is satisfied. If this program break-up condition is cancelled, the partition may become imbalanced again when maxiter is reached, because $h$ does not monotonically decrease in iteration process. The second is that, the proposed method is more proper for partitioning large-scale data set, because the quantity $\frac{W_i}{\bar{W}}$ in GeoClust can take high possibility to become very large and make the two related centers $c_i$ and $c_j$ move too long distance. This will lead to that the new data distribution between these two clusters is still very imbalanced. By modifying $\frac{W_i}{\bar{W}}$ to $\frac{l+1}{l+1} W_i$ $\frac{l+1}{l+1} W_j$, the movement degree of these two centers is controlled by parameter $l$. In order to compare the performance...
Equal clustering algorithm

Input: Data set \( \mathcal{X} = \{X_i\}_{i=1}^N, X_i \in \mathbb{R}^n \)  
Prescribed number of partition: \( m \)  
Maximum number of iterations: \( \text{maxiter} \)  
Learning parameters: \( \alpha \) and \( l \)  
The threshold of the value of object function: \( \varepsilon \)

Initialize: randomly choose \( m \) vectors in \( \mathcal{X} \), \( c_i^0, i = 1,2,\ldots,m \), as center vectors of each cluster \( m \) clusters \( C_i = \{c_i^0\}, i = 1,2,\ldots,m \)

Algorithm: For \( t=1: \text{maxiter} \)

1. Assign each sample \( X_j \in \mathcal{X} \) to the cluster nearest according to the distances between this sample and all center vectors. At the same time, the label indices of cluster that this sample belong to are recoded:
   \[
   \text{subcluster label}(j) = \arg \min_{m_{i+1}} \| X_j - c_i^{t-1} \|, j = 1,2,\ldots,N
   \]
2. Compute the numbers of samples in each cluster: \( W_1, W_2, \ldots, W_m \)
3. Compute the value of object function \( h \)
4. If \( h < \varepsilon \), then break
5. For each cluster \( C_i \) \( (i = 1,2,\ldots,m) \), Update its center as follows:
   \[
   \delta_i = \sum_{j=1, j \neq i}^{m} \left( \frac{W_j}{W_i + (t-1)W_i} - 1 \right) (c_j^{t-1} - c_i^{t-1})
   \]

6. End

End

Fig. 2. Equal clustering algorithm

<table>
<thead>
<tr>
<th>Problems</th>
<th>#attributes</th>
<th>#class</th>
<th>#training data</th>
<th>#test data</th>
<th>( c )</th>
<th>( \sigma )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Banana</td>
<td>2</td>
<td>2</td>
<td>40000</td>
<td>49000</td>
<td>316.2</td>
<td>0.707</td>
</tr>
<tr>
<td>Letter recognition</td>
<td>16</td>
<td>2</td>
<td>15000</td>
<td>5000</td>
<td>16</td>
<td>4</td>
</tr>
</tbody>
</table>

The problem statistics and the parameters used in SVMs.

of these two cluster methods, a quantity of \( h \times \text{iternum} \) is introduced, where the variable \( \text{iternum} (\text{iternum} \leq \text{maxiter}) \) means the number of iteration in each partitioning. Obviously, the smaller the quantity \( h \times \text{iternum} \) is, the better performance the algorithm gets. The performance comparison between GeoClust and the proposed equal clustering method is shown in Fig. 3. It can be seen that the proposed cluster method performs better than GeoClust.

IV. EXPERIMENTS

A. Experimental Setup

In order to evaluate the performance of the proposed clustering algorithm, simulation experiments are performed to compare the performances of \( M^3 \)-SVMs using random partition and equal clustering partition. The first data set is Banana data set that comes from [14] and the second one is Letter recognition data that comes from UCI [15]. For banana data, all 100 of its realizations are united to construct a large training data set and one realization of its test data is randomly chosen as test data set. Letter recognition problem is transformed into a two-class classification problem by the method like in [16]. The classes of \( "E", "H", "T", "M", "P", "Q", "R", "X", "Y", \) and \( "Z" \) are randomly set to positive class while the rest classes are set to negative class. The training and test data are normalized in the range \([0,1]\). From our experience, the data of these two experiments are not identically distributed. The problems statistics and the selection of the parameters for SVMs are shown in Table I.

In this paper, libSVM [17] whose cache is set to 100M is selected as training tool. All the experiments are performed on a PC that has 3.0GHz CPU with 1GB RAM. The kernel used is the radial-basis function, \( \exp(-\gamma \| X - X_i \|^2) \). For simplicity, we let \( K^+ = K^- = K \) in \( M^3 \)-SVM method. In order to systematically evaluate the proposed method, the value of \( K \) is set to 2,3,\ldots,20 in these experiments. \( K = 1 \) means that the classifier is trained by the entire training data. The training time of min-max modular support vector machines is counted in two ways. One is sequential training time that is the sum of the training time of all subclassifiers, and the other is parallel training time that is the longest training time among all the
classifiers. In order to ensure the credibility of the conclusions, all experiments are repeated three times and the average is taken.

B. Experimental Results and Discussions

In all the figures below, “RP” means random partition method and “CE” means equal clustering method. For convenience, M3-SVM-RP denotes min-max modular support vector machine based on random partition method, while M3-SVM-CE denotes min-max modular support vector machine based on equal clustering method.

From Fig. 4, it can be seen that the generalization ability of M3-SVM is better than standard SVM. The most interesting phenomenon is that M3-SVM-CE takes higher generalization accuracy than M3-SVM-RP does in most of time. Fig. 5 illustrates that M3-SVM-CE generates less support vectors than M3-SVM-RP does. In Fig. 6, even considering the time used in data partition shown in Table II, M3-SVM-CE takes less time than M3-SVM-RP does in sequential mode. From Table II, it can be seen that if the data partition time is ignored, M3-SVM-CE can run faster than M3-SVM-RP does in parallel mode. The reason is that CE can make the classification subproblems more separable than RP does. On the other hand, even though the data partitioning costs some time, the fewer support vectors and the higher generalization accuracy can compensate for it. The smaller the number of support vectors is, the less the test time and the cost of realization of M3-SVM are. In sum, equal clustering method makes min-max modular support vector machine more efficient than random partition does.

The reason of equal clustering method performs better than random partition method does can be explained from Figs. 7 and 8. When training data are random partitioned, all the classification subproblems look like the original classification problem as shown in Fig. 7. Therefore, all the subclassifiers will look alike and fail to complement each other. In comparison, all the classification subproblems focus on local feature space when training data are partitioned by equal clustering.

<table>
<thead>
<tr>
<th>Data</th>
<th>Data partition method</th>
<th>Average time per partitioning (s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Banana</td>
<td>CE</td>
<td>90.1</td>
</tr>
<tr>
<td>Letter</td>
<td>RP</td>
<td>1.5</td>
</tr>
</tbody>
</table>

The subclassifiers are so diverse that the two “min” and “max” integration principles works effectively. So the generalization accuracy of M3-SVM-CE is higher than M3-SVM-RP in most of time. When training data is not identically distributed in feature space, random partition will make the two class samples in each subproblem mix much more while equal clustering method will decrease the mixture degree of two class samples in each subproblem and enhance the separability of two classes in it. Therefore, the number of support vectors can be reduced and the training time is shortened. According to Vapnik [18], the decrease of support vectors will often promote the accuracy of support vector machines.

V. Conclusions

In this paper, a new clustering method is proposed to decompose large training data set into a number of smaller subsets. The feature of the proposed equal clustering method
is that it can partition data set more balancedly than GeoClust does. It has been observed that equal clustering method can catch local probability distribution information in training data, which is ignored by the random task partition method. The simulation results show that when training data are not identically distributed, the proposed clustering method will make min-max modular SVMs more efficient than the random task partition method does.

ACKNOWLEDGMENTS

This work was supported in part by the National Natural Science Foundation of China via the grants NSFC 60375022 and 60473040. The authors thank Yang Yang for useful advices.

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