Chapter 1
A Parallel and Modular Pattern Classification Framework for Large-Scale Problems

Bao-liang Lu\textsuperscript{1,2} and Xiao-lin Wang\textsuperscript{1}

\textsuperscript{1}Center for Brain-Like Computing and Machine Intelligence
Department of Computer Science and Engineering
\textsuperscript{2}MOE-Microsoft Key Laboratory for Intelligent Computing and Intelligent Systems
Shanghai Jiao Tong University
800 Dong Chuan Rd., Shanghai 200240, China
blu@sjtu.edu.cn

The number of samples that are available on the internet to train pattern classifiers is increasing rapidly, while traditional pattern classification techniques based on a single computer system are powerless to process these large-scale data sets. This chapter presents a parallel and modular pattern classification framework for coping with large-scale pattern classification problems. The proposed framework follows a divide-and-conquer strategy that easily assigns a given large-scale problem to an available parallel and distributed computing infrastructure. The framework consists of three independent parts: decomposing training data sets, training component classifiers in a parallel way, and combining trained component classifiers. In order to evaluate the performance of the proposed framework, we perform experiments on a large-scale Japanese patent classification problem, containing about 3,500,000 patent documents. The experimental results show that our framework has the following attractive features: (a) The framework is general, and therefore any traditional pattern classification techniques such as support vector machines can be easily embedded in the framework as component classifiers. (b) The framework can incorporate explicit domain or prior knowledge into learning through the process of dividing training data sets. (c) The framework has good scalability and is easily implementable in hardware.

1 Introduction

More and more large-scale classification problems appear in the field of machine learning and pattern recognition. By large-scale we mean that the training set is extremely large, typically to such an extent that traditional classifiers cannot finish the learning task within a bearable time. For example, recently, the training of support vector machines (SVMs) on large real-world data sets is reported to take several weeks. With the emergence of these large-scale classification problems, the efficiency of classifiers, besides accuracy, has become a subject of great focus.
A large-scale classification problem has huge time and memory costs. The ultimate solution to reducing time and memory costs is parallelism, that is, splitting one large-scale classification task among several CPUs, by which the system can meet an expected efficiency requirement. Unfortunately, most traditional classifiers are sequential in spirit, so we have to expend great efforts in parallelizing them. Recently, several parallel implementations of SVMs have been released [8, 4, 14, 34, 26, 13]. There are also parallel implementations of other classifiers, such as \( k \)-NN [3].

A very useful technology for these large-scale classification problems is ensemble learning. It employs a group of classifiers for a classification task, instead of one single classifier. Ensemble learning aims to achieve high accuracy, and it shows great efficiency in large-scale problems. Some of the ensemble learning methods require the sub-classifiers to be trained sequentially, while the others allow parallel training sub-classifiers. For methods such as Adaboost, the training set of a sub-classifier relies on feedback from previous trained sub-classifiers, and thus parallel learning is infeasible. As for other parallel ensemble learning methods, they are ideal solutions for large-scale tasks.

In this chapter, we introduce a parallel and modular pattern classification framework, named min-max modular network (M\(^3\)-network) [20, 21, 24]. This framework is a kind of a parallel ensemble learning method. First we train component classifiers on the subsets of the original data set. Then we make these component classifiers produce predictions on the arriving test sample. In the end we integrate all the predictions by two module combination rules, namely the minimization principle and the maximization principle.

To solve a large-scale multi-class classification problem, the M\(^3\)-network consists of three main steps: (a) Decompose the original multi-class problem into two-class problems and further divide the two-class problems which are difficult to be learned into a series of relatively smaller and balanced two-class subproblems. (b) Train all the two-class subproblems in parallel. (c) Combine all the trained component classifiers into a hierarchical, parallel, and modular network that serves as the solution to the original problem.

Many studies prove that M\(^3\)-network is an efficient classifier, especially in solving large-scale and complex pattern classification problems [22, 10, 32, 19, 5, 6]. M\(^3\)-network has the following three advantages over traditional pattern classification approaches: (a) A large-scale and complex multi-class problem can be decomposed to two-class subproblems as small as the user expects. (b) The two-class subproblems are independent to each other, therefore, they can be solved in parallel without the trouble of communication. (c) The two module combination principles are simple, which are easily implementable in software and hardware.

2 Min-Max Modular Network

Lu and Ito proposed the Min-Max Modular Network (M\(^3\)-network for short) in order to solve hard classification problems in 1997 [20, 21]. M\(^3\)-network is a sort
of ensemble learning methods that employs a group of classifiers for one classification problem. The $M^3$-network follows the principle of divide and conquer, dividing the whole problem into small pieces and solving them one by one, and adopts a 3-step workflow: task decomposition, training component classifiers and module combination (see Figure 1).

Before formally describing the $M^3$-network, we would like to present an illustration (Figure 2) [25]. Suppose that subfigure (a) is the two-class classification problem that needs to be solved, where small red disks represent positive samples and small blue rectangles represent negative ones. Though simple at first sight, it’s actually a non-linearly separable problem. To demonstrate $M^3$-network learning, we divide samples of each class into two subsets, surrounded by dashed lines in subfigure (a). According to this partition of the training data set, we generate four smaller classification subproblems shown in subfigures (b) to (e). Then we train classifiers on these subproblems, where dashed lines represent the discriminant surfaces. After that we derive separately subfigures (f) and (g) from subfigures (b) through (e) with the minimization operator, resulting in negative zone expanding. Finally, we derive subfigure (h) from subfigures (f) and (g) with the maximization operator, resulting in positive zone expanding. From subfigure (h), it is obvious that we find the correct discriminant plane to the classification problem.

### 2.1 Task Decomposition

Let $T$ denote the training data set for a $K$-class classification problem,

$$T = \{(X_i, Y_i)\}_{i=1}^L$$  \hspace{1cm} (1)
where \( X_i \in \mathbb{R}^d \) is the training input, \( Y_i \in \mathbb{R}^K \) is the corresponding desired output, and \( L \) is the total number of training samples.

At the beginning of the task decomposition process, a large-scale \( K \)-class classification problem is divided into a series of relatively smaller two-class subproblems by using a one-versus-one or one-versus-rest task decomposition strategy. Suppose a \( K \)-class classification problem is decomposed by a one-versus-one strategy into the following \( K(K - 1)/2 \) two-class subproblems:

\[
T_{ij} = \{(X^i_l, +1)\}_{l=1}^{L_i} \cup \{(X^j_l, -1)\}_{l=1}^{L_j}
\]

for \( i = 1, \ldots, K \) and \( j = i + 1, \ldots, K \)

where \( X^i_l \in \mathcal{X}_i \) and \( X^j_l \in \mathcal{X}_j \) are the training inputs belonging to class \( \mathcal{C}_i \) and class \( \mathcal{C}_j \), respectively; \( \mathcal{X}_i \) is the set of training inputs belonging to class \( \mathcal{C}_i \); \( L_i \) denotes the number of data in \( \mathcal{X}_i \); \( \bigcup_{i=1}^{K} \mathcal{X}_i = \mathcal{X} \); and \( \sum_{i=1}^{K} L_i = L \). In this chapter, the training data in a two-class problem are called positive training data if their desired outputs are +1, and they are called negative training data if their desired outputs are −1.

Even though the two-class problems defined by Eq. (2) are smaller than the original \( K \)-class problem, this partition may be not adequate for parallel learning. Since the number of samples in each class varies largely, the sizes of these two-class problems can be quite different. Thus the training period can be delayed by some larger two-class problems. A large class and a small class together form an imbalanced classification problem; there are too many samples on one side, which increases the difficulty in training classifiers [2]. To speed up training and to improve classification accuracy, all the large and imbalanced
two-class problems are further divided into smaller and more balanced two-class problems.

Assume that $\mathcal{X}_i$ is partitioned into $N_i$ subsets in the form

$$\mathcal{X}_{ij} = \{X_{ij}^{li}\}_{i=1}^{L_i}$$

for $j = 1, \cdots, N_i$ and $i = 1, \cdots, K$,

where $1 \leq N_i \leq L_i$ and $\bigcup_{j=1}^{N_i} \mathcal{X}_{ij} = \mathcal{X}_i$.

After partitioning $\mathcal{X}_i$ into $N_i$ subsets, every two-class problem $\mathcal{T}_{ij}$ defined by Eq. (2) is further divided into $N_i \times N_j$ smaller and more balanced two-class subproblems:

$$\mathcal{T}_{ij}^{(u,v)} = \{(X_{iu}^{(iu)}, +1)\}_{i=1}^{L_i^{(u)}} \cup \{(X_{jv}^{(jv)}, -1)\}_{i=1}^{L_j^{(v)}}$$

for $u = 1, \cdots, N_i$, $v = 1, \cdots, N_j$, $i = 1, \cdots, K$, and $j = i + 1, \cdots, K$,

where $X_{iu}^{(iu)} \in \mathcal{X}_{iu}$ and $X_{jv}^{(jv)} \in \mathcal{X}_{jv}$ are the training inputs belonging to class $C_i$ and class $C_j$, respectively; $\sum_{u=1}^{N_i} L_i^{(u)} = L_i$ and $\sum_{v=1}^{N_j} L_j^{(v)} = L_j$.

2.2 Training Component Classifiers

After task decomposition, all of the two-class subproblems are treated as completely independent, non-communicating tasks in the learning phase. Therefore, all the two-class subproblems defined by Eq. (4) are efficiently learned in a massively parallel way.

From Eqs. (2) and (4), we see that a $K$-class problem is divided into

$$\sum_{i=1}^{K-1} \sum_{j=i+1}^{K} N_i \times N_j$$

two-class subproblems. The number of training data for each of the two-class subproblems is approximately

$$[L_i/N_i] + [L_j/N_j],$$

where $[z]$ denotes the smallest integer than or equal to $z$. Since $[L_i/N_i] + [L_j/N_j]$ is independent of the number of classes, $K$, the size of each two-class subproblems is much smaller than the original $K$-class problem for the reasonable values of $N_i$ and $N_j$.

Traditional machine learning algorithms and pattern classification approaches such as multilayer neural networks [21], support vector machines [23] and $k$-nearest neighbor algorithm [35], can be used to learn the two-class subproblems defined by Eq. (4). In this chapter, most commonly used SVMs are selected as component classifiers and used to learn all of the two-class subproblems.
2.3 Module Combination

After all of the two-class subproblems defined by Eq. (4) have been learned by SVMs, all the trained SVMs are integrated into a \( M^3 \)-SVM with the Min and Max units according to the minimization principle and maximization principle [23]. The function of the Min unit is to find a minimum value from its multiple inputs. The transfer function of the Min unit is given by

\[
q(x) = \min_{i=1}^{P} M_i(x)
\]  

(7)

where \( x \) denotes the input variable. The function of the Max unit is to find a maximum value from its multiple inputs. The transfer function of the Max unit is given by

\[
q(x) = \max_{i=1}^{P} M_i(x)
\]  

(8)

**Minimization Principle:** Suppose a two-class problem \( \mathcal{B} \) is divided into \( P \) smaller two-class subproblems, \( \mathcal{B}_i \) for \( i = 1, \cdots, P \), and also suppose that all the two-class subproblems have the same positive training data and different negative training data. If the \( P \) two-class subproblems are correctly learned by the corresponding \( P \) individual SVMs, \( M_i \) for \( i = 1, \cdots, P \), then the combination of the \( P \) trained SVMs with a Min unit will produce the correct output for all the training inputs in \( \mathcal{B} \).

**Maximization Principle:** Suppose a two-class problem \( \mathcal{B} \) is divided into \( P \) smaller two-class subproblems, \( \mathcal{B}_i \) for \( i = 1, \cdots, P \), and also suppose that all the two-class subproblems have the same negative training data and different positive training data. If the \( P \) two-class subproblems are correctly learned by the corresponding \( P \) individual SVMs, \( M_i \) for \( i = 1, \cdots, P \), then the combination of the \( P \) trained SVMs with a Max unit will produce the correct output for all the training input in \( \mathcal{B} \).

Note that the module combination strategy based on the minimization and the maximization principles is called the min-max module combination in this chapter. Figure 3 illustrates the min-max module combination for a two-class problem. Here the two-class problem is first decomposed into \( N_1 \times N_2 \) two-class subproblems. Then each component classifier is trained on the corresponding two-class subproblem. Finally a \( M^3 \)-network is constructed by combining these component classifiers. In this case, the \( M^3 \)-network consists of \( N_1 \) Min units, and one Max unit.

3 Parallel Implementation of \( M^3 \)-network

As a principle, improvement in both the feasibility and the efficiency of parallelizing in a computation process is inverse to communication among its high-level parts. The \( M^3 \)-network is highly modular, that is, it has clear modules with almost no communication among them, except the final step of combining multiple results. Therefore, it is natural and efficient to run these modules simultaneously, that is, to parallelize \( M^3 \)-network.
Fig. 3. Illustration of min-max module combination for a two-class problem.

3.1 Parallel Training of M³-network

The parallel implementation of M³-network is based on its modular structure. In the training phase, we first distribute subproblems among the computer nodes, then the nodes train component classifiers independently, and finally we collect all the trained component classifiers to finish training. In the test phase, we first distribute component classifiers, namely modules, among computer nodes, then we send the test samples to nodes and receive predictions from them, and finally we get the final predictions of the test samples through both minimization and maximization operations.

Figure 4 illustrates the parallel framework for training M³-network. From the viewpoint of parallel programming, M³-network falls into the category of pleasant parallel problems, and therefore master-slave framework is recommended for this category [29].

In the training phase, we need to provide each slave node with samples, which have long input vectors in large volumes. If we store all of the samples in the master node and then later send them into the slave nodes together with the subproblems, the master node will become a bottleneck for data transfer. As a solution, we distribute the samples into slave nodes that can communicate with one another through point-to-point communication. Thus, in assigning the subproblems, the master node only needs to send the slaves nodes the indexes of the samples, which greatly reduces the communication load.

Figure 5 illustrates the parallel framework of M³-network in test phase. In the test phase, the operation of either minimization or maximization can be done with one call to MPI_Reduce procedure in MPI programming environment, which is well designed and works acceptably fast [29].
**Fig. 4.** The parallel framework for training M$^3$-network.

**Fig. 5.** The parallel framework of M$^3$-network in test phase.
3.2 Asymmetric and Symmetric Module Selection Strategies

The symmetric module selection strategy is an improved version of the min-max module combination method, namely asymmetric module selection strategy. This strategy works exponentially faster. Its main disadvantage is that it must work on concrete classifiers which output either 0 or 1, instead of continuous confidence values in the min-max module combination.

Let us review the min-max module combination method, and explain why we call it the asymmetric module selection strategy. Suppose the outputs of all of the modules on a test sample are positive 1 or negative 0 (see Figure 6(a)). Following the min-max module combination method, we first perform minimization operation along each row, then perform maximization operation among the rows’ results. The final result is 1 in this example. Note that this result is caused by the fourth row, full of 1’s as its elements. The translation of this process in feature space is that the test sample input is located within the subset $X_{4}$, so that it shows positive in all the subproblems $T_{ij}(k = 1, 2, \ldots, 5)$. The logical definition of the min-max module combination for $M^3$-network is:

- If there exists a row of all 1 in module’s prediction matrix, the output is 1;
- Otherwise, the output is 0.

The min-max module combination method has a bias towards the output of 0, and that is why we call it asymmetric module selection.

The other combination method, the symmetric module selection strategy, is illustrated in Figure 6(b) [36]. In this method, we start from the top left element. If the element is 1, we go one step right; otherwise, we go one step down. The process continues until we go beyound the boundaries of the matrix. If we pass through the right edge of the matrix, the method outputs 1; otherwise, it outputs 0. The logical definition of this method is:

- If there exists a row of all 1 in module’s prediction matrix, the output is 1;
- If there exists a column of all 0, the output is 0;
- Otherwise, the output can be either 1 or 0.

The third case is rare in solving regular pattern classification problems with $M^3$-network, and it doesn’t need to be considered [36]. From the viewpoint of feature space, the first case means that the test sample input is located within some positive subsets, and the second case for some negative subsets, so this method make sense. Moreover, this method has no bias towards either 1 or 0, that is why we call it a symmetric module selection. Indeed, this characteristic makes it likely to perform better than the asymmetric module selection method.

The symmetric module selection strategy has a great advantage on computation complexity, compared with the asymmetric one. Suppose the training data sets for two classes are divided into $m$ and $n$ subsets, respectively. The complexity of the asymmetric module selection is $O(mn)$, and that of symmetric module selection is $O(m + n)$; so it is clear the symmetric module selection is one order faster than the asymmetric module selection. Further, the component classifiers
that are not visited do not need to be actually computed (see Figure 6), that is, the module combination method determines the complexity of whole test process of M³-network. For these two reasons, the new symmetric module selection method can greatly accelerate the response speed of M³-network, which is our main purpose.

3.3 Parallel Implementation of Symmetric Module Selection

A kind of communication exists among the modules by symmetric module selection, that is, whether a module needs to be run depends on the output of some other modules. Though we can ignore such dependency and run all the modules with the master-slave framework adopted in Section 3.1, it is not a wise choice.

The parallel pipeline framework shown in Figure 7 fits this context well. In a pipeline, some nodes do partial processing of data and then forward the partially processed results to another processing nodes down the pipeline for further processing [29].

The key issue of applying the pipeline framework is to design the task for each stage. To implement M³-network in the style of a pipeline, we decompose the matrix of modules along the reverse diagonals; then take the modules in the same reverse diagonal as one stage, and number them from 1 to $n + m + 1$, the same as the distance to the top-left cell (see the nine dotted lines in Figure 8) [33].

We build M³-network by assigning some computer nodes to run the modules in each reverse diagonal. After that we start the system by inputting a test sample with a position status of $(1, 1)$, to a computer node that is in charge of the first reverse diagonal. All the successive steps are iterative. When the test sample with the position status $(r, c)$ arrives at the $(r+c-1)$th reverse diagonal, a computer node of that diagonal first runs the module $M_{ij}^{(r,c)}$ corresponding to the two-class subproblem $T_{ij}^{(r,c)}$. Then it updates the sample’s position status with $(r, c + 1)$ if the module outputs 1, or with $(r + 1, c)$ otherwise. At last it passes this sample to the next reverse diagonal. The advantage of such stage
Fig. 7. Illustration of the pipeline framework

The design is that each computer node can complete its job by running exactly one module, which simplifies workload balancing.

Fig. 8. Design of a pipeline for $M^3$-network

The number of computer nodes assigned to each reverse diagonal should agree with the number of arriving samples, for the sake of workload balance. Considering that samples leave the matrix from the right and bottom edges, from 1st to $\min(n, m)$-th reverse diagonals, the number of computer nodes should be fixed; after that, the number should gradually decrease.
4 Application to Patent Documents Classification

Patents, as a social innovation system, have been an increasingly important role in science and technology improvement. As a result, automatic patent classification, as a basic data mining technique on patents, has received wide attention. A number of organizations including the European Patent Office, the Japanese Patent Office, and companies have been working on this topic [9, 12].

4.1 Patent Documents Classification

Patent documents classification takes the standard of the International Patent Classification (IPC) as a label system [12]. IPC is a complex hierarchical symbol system, where all the technological fields are divided into 8 Sections, 120 Classes, 630 Subclasses and approximately 69,000 Groups. We use M$^3$-network to classify Japanese patent documents on the Section level of the International Patent Classification taxonomy, which is a very large classification task [25].

We work on a Japanese patent corpus called the Japanese National Information Institutes’ Testing Corpus for Information Retrieval (NTCIR), which is publicly available for research purpose\(^1\). The corpus consists of about 3,500,000 documents of Japanese patent applications from 1993 to 2002. A patent document is a structured text with one title and three fields, Abstract, Claim and Description (see Table 1).

![Fig. 9. Illustration of the IPC taxonomy. Here, ‘A’ is the Section category label, ‘A01’ is the Class category label, ‘A01B’ is the Subclass category label, and ’A01B 13/08’ is the Group category label.](image-url)

\(^1\) http://research.nii.ac.jp/index-en.html
4.2 Task Decomposition with Prior Knowledge

Using hints greatly improves the effects of machine learning [1]. In this application we make use of the patents’ hints, publish dates and hierarchical labels, to perform the task decomposition for $M^3$-network. The decomposition process, namely $M^3$-YC, consists of the following three steps (see Figure 10).

**step 1** Divide the training data set of each Section by publish dates, each subset for one year;

**step 2** Further divide the subsets by class, thus each subset for one Class published in one year;

**step 3** Further randomly divide the remaining large subsets into smaller fix-sized subsets.

Note that with steps 1 and 2 removed, the above process becomes the standard $M^3$-network, namely $M^3$-Rand. In this research, our main concern is $M^3$-YC, and we take $M^3$-Rand and plain SVMs as the baseline methods.

In both $M^3$-Rand and $M^3$-YC, we can control the size of subproblems through the step of random decomposition, for example, setting the maximum number of samples in a subset. We must keep the subproblems in moderate size, neither too large for a single classifier to learn, nor so small that there are too many little subproblems. We finally decide on the maximum size of a subset to be 2000 samples, according to some pilot experiments.
Fig. 10. Illustration of task decomposition with prior knowledge. Different attributes among the samples are shown by colors and shapes. The colors correspond to publish dates: red samples published in the same year and blue ones in another. The shapes correspond to the sub-categories: rectangles and triangles for two sub-categories of category A, and the circles and diamonds for two sub-categories of category B. The task decomposition consists of three steps, first by the prior knowledge of the publish year (b), and then by the Class category (c), and last by random for remaining large subsets (d).
4.3 Experiment Settings

Training and Test Data Sets  We have an extended version of NTCIR-5 Japanese patent corpus at hand, which consists of all the patent applications published by the Japanese Patent Office from 1993 to 2002. In order to truthfully evaluate the three methods, conventional SVMs, M3-Rand and M3-YC, we make eight pairs of training and test data sets, creating a real-world context (see Table 2).

<table>
<thead>
<tr>
<th># of years for training</th>
<th>years</th>
<th>set size</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>training</td>
<td>test</td>
</tr>
<tr>
<td>1</td>
<td>2000</td>
<td>2001,2002</td>
</tr>
<tr>
<td>2</td>
<td>1999,2000</td>
<td>2001,2002</td>
</tr>
<tr>
<td>4</td>
<td>1997–2000</td>
<td>2001,2002</td>
</tr>
</tbody>
</table>

Feature extraction and filtering  Several steps of preprocessing need to be done before getting the vector representation of the Japanese text used by classifiers. These steps are tokenization, term filtering, and term indexing.  

Tokenization generates a list of clean and informative words from raw text. We first extract the raw text from the four patent fields, Title, Abstract, Claim and Description (see Table 1), as they are most informative about the patent's content. Then we segment these texts into isolated words using the software Chasen<sup>2</sup>. After that, we remove the stop words (or empty words) from the results. The remaining words, namely terms in the research domain of text categorization, are features for the successor classification task. Table 3 shows the result we get from the example shown in Table 1.

Table 3. The terms of a Japanese patent document shown in Table 1

<table>
<thead>
<tr>
<th>terms</th>
</tr>
</thead>
<tbody>
<tr>
<td>土壌(soil) 改良(improve) 方法(methods) 作業(working) 機(machine) % title</td>
</tr>
<tr>
<td>心土(subsoil) 破砕(crack) 雪上(snow) 心土 破砕 作業 ...% abstract</td>
</tr>
<tr>
<td>サブソイラ(subsoiler) 作業 機 心土 破砕 作業 ...%claim</td>
</tr>
<tr>
<td>発明(patent) 土壌 改良 方法 ...%description</td>
</tr>
</tbody>
</table>

<sup>2</sup> http://chasen.naist.jp/hiki/ChaSen/
Term Filtering removes the useless terms in the classification task. This shortens the length of the representation vectors, and thus cuts the computational cost and reduces generalization errors. We take $\chi^2_{avg}$ as filtering criterion [31]), and pick up 5000 top terms as features, according to our pilot experiments. Table 4 shows the top 10 terms sorted by $\chi^2_{avg}$, most of which are technical terms representing patent documents.

<table>
<thead>
<tr>
<th>terms explanation</th>
<th>$\chi^2_{avg}$</th>
<th>terms explanation</th>
<th>$\chi^2_{avg}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>data</td>
<td>10384.72</td>
<td>article</td>
<td>7528.72</td>
</tr>
<tr>
<td>information</td>
<td>10199.42</td>
<td>contain</td>
<td>7374.12</td>
</tr>
<tr>
<td>circuit</td>
<td>9561.67</td>
<td>connect</td>
<td>7324.43</td>
</tr>
<tr>
<td>signal</td>
<td>8387.75</td>
<td>insulation</td>
<td>7194.85</td>
</tr>
<tr>
<td>record</td>
<td>7901.17</td>
<td>baseplate</td>
<td>7076.72</td>
</tr>
</tbody>
</table>

Term Indexing generates the weights of feature terms for a sample with the real numerical vectors. We adopt the dominant methods of TFIDF [27].

$$
tfidf(t, d) = n(t, d) \log \frac{|T_r|}{n_{T_r}(t)}
$$

(9)

where $t$ denotes a term, $d$ denotes a document, $T_r$ denotes the training corpus, $n(t, d)$ denotes the number of times $t$ occurs in $d$, namely term frequency, and $n_{T_r}(t)$ denotes the number of documents where $t$ occurs, namely document frequency. Table 5 shows the vector representations of selected patent documents.

<table>
<thead>
<tr>
<th>No.</th>
<th>Vectors</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>72 : 0.730 98 : 1.790 138 : 1.310 141 : 4.495 ...</td>
</tr>
<tr>
<td>3</td>
<td>71 : 1.463 79 : 2.441 85 : 2.993 113 : 11.393 ...</td>
</tr>
<tr>
<td>4</td>
<td>42 : 2.164 60 : 0.905 109 : 2.061 138 : 2.947 ...</td>
</tr>
<tr>
<td>5</td>
<td>28 : 7.529 72 : 6.577 139 : 8.103 167 : 8.728 ...</td>
</tr>
</tbody>
</table>

Computational Platform A Lenovo cluster system consisting of three fat nodes and thirty thin nodes run all of our experiments. Each fat node has 32 GB of RAM and two 3.2-GHz quad-core CPUs, while each thin node has 8 GB of RAM and two 2.0-GHz quad-core CPUs. Experiments with the conventional SVMs were performed on the fat nodes because they need large memory, while experiments with the M$^3$-network were done on the thin nodes because each sub-problem was small and a lot of processors were required for parallel training.
Training Component Classifier} M^3-network is a general framework for pattern classification. The user can select suitable component classifiers according to the classification task to be solved and available computing resource. There are several alternative choices, such as multilayer neural networks[21], k-nearest-neighbor algorithm[35, 30], and SVMs [23]. Here we select conventional SVMs with linear kernel and use SVM^{light}, an implement of SVM by Joachims [15]. SVM^{light} actually plays two roles in this chapter, the baseline method and the component classifiers for M^3-network.

Performance Measurement} The conventional measurement of accuracy in machine learning domain makes less sense for most text categorization tasks; instead, we usually use the function $F_1$ [27]. The formula of $F_1$ of one class is:

$$F_1 = \frac{2PR}{P + R}$$  \hspace{1cm} (10)

$$P = \frac{TP}{TP + FP}$$  \hspace{1cm} (11)

$$R = \frac{TP}{TP + FN}$$  \hspace{1cm} (12)

where $TP$ is the number of classifier’s True Positive predictions, $FP$ for False Positive, and $FN$ for False Negative. $P$ is named the precision, and $R$ is named the recall. In practice, there are the two following versions of $F_1$, depending on the methods of integrating individual results:

$$micro - F_1 = \frac{2PR}{P + R}$$  \hspace{1cm} (13)

$$macro - F_1 = \text{avg} \frac{2P_cR_c}{P_c + R_c}$$  \hspace{1cm} (14)

where $P$ and $R$ are computed with all the classes, while $P_c$ and $R_c$ are computed on only class $c$. For example, sample $s$ actually belongs to classes $c_1$ and $c_2$, while the classifier’s predictions is $c_2$ and $c_3$. Then in computing $micro - F_1$, $TP$, $FP$ and $FN$ will be increased by 1, while in computing $P_{c1}$ and $R_{c1}$ for $macro - F_1$, only $FN$ will be increased by 1.

4.4 Results and Discussions

Accuracy} Figure 11 is the experimental results, with $micro-F_1$ and $macro-F_1$ used as accuracy measurements. The following conclusions can be drawn from our results:

(a) On the aspect of test accuracy, the two M^3-SVM methods, M^3-Rand and M^3-YC, are both superior to conventional SVMs. We can learn from the training scores that conventional SVMs with linear kernel are unable to learn the training set completely, because its $micro-F_1$ and $macro-F_1$ are
only about 80%. On the contrary, as an ensemble learning algorithm, M$^3$-SVMs can generate a powerful classifier by combining simple classifiers. As a result, M$^3$-SVMs have fulfilled the learning on all the training sets with accuracies of nearly 100%.

(b) M$^3$-Rand and M$^3$-YC show superior robustness to conventional SVMs over dated samples. Along the moving backward of the starting time point of training set, more and more dated samples are added, thus the performance of conventional SVMs decreases. Contrarily, the performance of two M$^3$-SVMs increases at the same time. Though their performance decreases a little in the 5th year point and 7th year point. This does not affect the curves’ overall trend.

(c) M$^3$-YC over-performs M$^3$-rand on each year point, which indicates that incorporating prior knowledge of the publishing date and the Class category into task decomposition will undoubtedly improve classification performance.

**Time Cost** As mentioned before, M$^3$-SVMs (both M$^3$-Rand and M$^3$-YC) have the merit of parallel computing, which greatly speeds up learning. However, we are sharing the Lenovo parallel computer system with other users while performing the experiments, so the accurate time cost of M$^3$-SVMs could not be measured. The time cost of conventional SVMs has been recorded as it didn’t involve parallel running.

We evaluate the time cost of M$^3$-YC using the following formula:

\[
t_{M^3} = \frac{n_{mod} \times t_0}{n_{cpu}}
\]

where $n_{mod}$ is the number of modules (or subproblems), $t_0$ is the average time cost of per module, and $n_{cpu}$ is the number of CPUs. During our experiments, $n_{mod}$ have been recorded automatically and $n_{cpu}$ is 30 on the Lenovo cluster system. As for $t_0$, it must be measured by experiment, and the eventual value we get is 0.025 seconds per module.

Figure 12 is the time costs of conventional SVMs and M$^3$-YC in our experiments. From this figure, we can know that the M$^3$-YC’s time cost is only about 1/10 of the SVM’s, which agrees with our expectation well.

5 Conclusions

In this chapter, we present a parallel and modular pattern classification framework for large-scale problems. The framework works in a modular manner, and has several advantages in solving large-scale problems. On the one hand, massively parallel and distributed training is easily implementable because of its modularity. On the other hand, it has a balanced performance on all classes because of various task decomposition strategies.

The experiments are conducted on a large-scale Japanese patent corpus. Taking into account prior/domain knowledge, we partition large training data sets
Fig. 11. Performance comparison of conventional SVMs, M\textsuperscript{3}-Rand and M\textsuperscript{3}-YC: (a) micro-$F_1$ on test data; (b) macro-$F_1$ on test data; (c) micro-$F_1$ on training data; and (d) macro-$F_1$ on training data.
into smaller subsets according to the publishing date and the subclass. The experimental results show the effectiveness of the proposed framework, and demonstrate that M³-SVMs is superior to conventional support vector machines in solving such complex problems.

As more and more large-scale applications appear in the fields of machine learning and pattern recognition, there is greater need for parallel and distributed methods. M³-network uses simple task decomposition methods and efficient module selection strategies and can be implemented easily in practice. We recognize that incorporating prior/domain knowledge into task decomposition is a reliable way to improve the learning efficiency and the generalization performance of M³-network. We believe that the proposed parallel and modular framework will be very useful for solving complex classification problems with very large data sets.

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