Recognizing Slow Eye Movement for Driver Fatigue
Detection with Machine Learning Approach

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Abstract—Slow eye movement (SEM) regarded as a sign of
onset of sleep is very significant for detecting driver fatigue,
but its characteristics and detection algorithm have been rarely
involved in the study of driver fatigue detection. In this study,
some new features were extracted based on wavelet singularity
analysis and statistics to detect SEMs. Six subjects participated in
this simulated driving experiment, and for each subject, a more
than 2 hours electro-oculogram (EOG) session was recorded.
Each session was divided into SEM epochs and non-SEM epochs
according to the common judgments made by the two of three
experts by the visual recognition criteria of SEMs. Regarding
the problem of detecting SEMs as an imbalance classification
problem, and through the under-sampling and over-sampling
methods a 2s horizontal electro-oculogram (HEO) signal could
finally be recognized as the category of SEMs or non-SEMs with
the classifiers SVM, GELM, and KNN respectively. Results prove
that the proposed features was a little better than the wavelet
energy features, and through the combination of new features
and statistics, the classification results were improved
obviously.

I. INTRODUCTION

Slow eye movement (SEM) has been proved to be a reliable
indicator of sleep onset, and was studied in a number of
various kinds of sleep related researches [1, 2, 5, 7]. Because
SEM appears during the wake-sleep transition, so it is very
significant to study SEM in a real driving condition to avoid
traffic accidents.

Blinks, saccades and fixation are the main ways of eye
movements in wakefulness of human. The relationship be-
tween EOG and driver fatigue has been studied long time ago.
However, little attention is being given to the characteristics
of SEM about fatigue driving, and the specific description of
SEM, such as what is the eye state (open or closed?) when it
occurs, is insufficient. Our experiments found that SEM could
happen in the case of frequent continuous long blinks because
of feeling sleepy and most happened during the period with
eyes closed when people were in a state of severe drowsiness
and could not control the trend of drooping eyelids.

For overlong eye lid closures (more than 3 seconds), there
is no method to detect them. The conventional detection
method for EOG is only according to the waveform in vertical
electro-oculogram (VEO), but it can not distinguish it from an
upward glance followed by a downward glance [8, 9]. And in
the condition of serious squint, the waveform caused by eyes
closing and the following waveform caused by eyes opening
in VEO are not obvious and very difficult to recognize. For
the video detection method, it can not distinguish the driver’s
sleepy state from brief eye closure due to other reasons [10].
When the driver is awake and close his/her eyes, the SEMs
will not appear, but when the driver is very sleepy and closes
eyes at this movement, the SEM will appear in HEO [11, 12].
However, at this movement, the waveform of SEM in the HEO
is very clear and easy to recognize. So detecting SEMs in HEO
is very significant for judging the driver’s current fatigue state.

To detect driver fatigue, algorithms for automatic recog-
nizing SEMs have been rarely reported to our best knowledge.
In sleep research field, there exist some methods, but these
methods were not satisfactory. In 1999, a linear regression
method was used for the detection of SEM, and it was reported
that the cycle length of SEM was shorter at stage wake than
at sleep stages 1 and 2 [6]. In 2006, Elisa Magosso developed
a wavelet based method, which was under the assumption
that energy distribution was modified during SEM epochs
according to the observation of experimental data [3]. SEMs
could be detected through a discriminate function, which was
defined as the ratio of specific energy combinations at lower
frequencies with respect to both lower and higher frequency
components. In [5], it simply judged SEMs or non-SEMs by
the amplitude threshold and the mean velocity threshold in a
simulated driving task.

In essence, the previous work used the wavelet energy
features and statistics features to detect SEMs, but seldom
involved in the machine learning methods, in this study, new
features based on wavelet singularity analysis and statistics
such as entropy were proposed, and machine learning methods
are introduced. For the classification, Support vector machines
(SVMs) have been extensively used in widespread applications
and were proved to have good generalization ability. The
discriminative graph regularized Extreme Learning Machine
(GELM) also is used to improve the performance based on the
idea that similar samples should share similar properties and
were proved to achieve much performance gain over standard
ELM [13]. Therefore, by using these classifiers, our proposed
features and the existing wavelet energy features are evaluated
respectively. Experiments results found the performance of
the new proposed features was slightly better than wavelet
energy features. And through the combination of new features

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and wavelet energy features, the classification results can be improved obviously. This paper is organized as follows: In Section 2, the new features for recognizing SEMs are proposed, which are based on wavelet singularity analysis and statistics. And the overall processing procedure for classification using SVM, GELM and KNN is presented. Section 3 introduces the materials of the simulated driving experiments and gives a detail description of the characteristics of SEMs. Section 4 presents the experiments results and discussion. Section 5 concludes this work.

II. COMPUTER ANALYSIS PROCEDURE

The horizontal electro-oculogram (HEO) signal is calculated as the difference between the two convectional channels near the outer canthi of eyes. As can be seen in Fig. 1, one HEO signal session is divided into pieces of window data of length \( t = 2 \) seconds with a sliding step of length \( s, s \) and \( t \) could be set by user. For each window data, new features are defined and extracted based on wavelet transformation and other statistical parameters. By training classifiers, each window data will be classified as the category of SEMs or non-SEMs.

![Fig. 1. The chart of computer analysis procedure](image)

The labels of SEMs epochs and non-SEM epochs in HEO need to be marked manually. Eye movements were recognized as SEMs by visual experts if they meet the following criteria [3]: (1) slow sinusoidal excursion (0.2-0.6Hz) lasting more than one second; (2) amplitude between 20 and 200uV; (3) binocular synchrony with opposed-phase deflections in the two channels; (4) onsets of the right and left eye movement occur within 300ms of one another; (5) absence of artifacts; These criteria are commonly adopted for visual recognition of slow eye movements, which can be seen in Fig. 2. The rest HEO epochs which did not meet these criteria were labeled as non-SEMs. Then, the SEMs epochs and non-SEM epochs were divided into many 2s window data to form the original data samples.

A. New features

In this section, the features based on wavelet singularity analysis and some new statistics features are proposed.

1) wavelet transformation: The wavelet is a smooth and quickly vanishing oscillating function with good localization in both frequency and time [4]. A wavelet family \( \psi_{a,b}(t) \) is the set of elementary functions generated by dilations and translations of a unique admissible mother wavelet \( \psi(t) \):

\[
\psi_{a,b}(t) = \frac{1}{\sqrt{|a|}} \psi \left( \frac{t-b}{a} \right) \tag{1}
\]

where \( a, b \in \mathbb{R}, a \neq 0, \) \( a,b \) are the scale and translation parameters, respectively, and \( t \) is the time. If the parameters \( (a,b) \) are continuous value, the transform is called continuous wavelet transform. Otherwise, if the parameters are discrete such as \( a = a_0^j, b = k b_0 a_0^j \) that will be called the Discrete Wavelet Transform (DWT) basis as follows:

\[
\psi_{j,k}(t) = a_0^{-j/2} \psi \left( a^{-j} t - k b_0 \right), j, k \in \mathbb{F} \tag{2}
\]

If \( \psi_{j,k} \) constitute the orthogonal wavelet basis of \( L(\mathbb{R}) \), for a arbitrary signal sample \( f(t) \), the following equation exists:

\[
f_w(t) = \sum_j \sum_k C_j(k) \psi_{j,k}(t) \tag{3}
\]

where \( C_j(k) = \langle f_w(t), \psi_{j,k}(t) \rangle \)

2) Features based on wavelet singularity analysis: In digital signal processing, singularity detection of time series has important meaning, because these singularities contain the important information about the instantaneous change of signal [14, 15, 17]. Wavelet transform has a strong ability in detecting singularity and has been widely used. Because the eye movement is mostly a momentary behavior, and when saccades or blinks happen, the signal waveform will present some mutation points. However, the waveforms of SEMs are relatively smooth, without obvious mutation points. So, the continuous wavelet transform method for singularity analysis was chosen to identify SEMs in HEO.

\[
\psi(t) = \left( \frac{2}{\sqrt{3}} \pi^{-1/4} \right) (1-t^2) e^{-t^2/2} \tag{4}
\]

Mexican hat wavelet, as a commonly used wavelet base, its function (Eq. (4)) is proportional to the second derivative function of Gaussian probability density function, and has even symmetry structure, as can be seen in Fig. 3. If this function with even symmetry structure is used to do the convolution with an abrupt change point with local even symmetry, the convolution result will be local even symmetry. Otherwise, the result will be local odd symmetry.

Actually, continuous wavelet transform of the signal with Mexican hat mother wavelet is equal to making convolution
between the signal and Mexican hat wavelet with the scaled and translated variables. For Mexican hat mother wavelet function (Eq. (4)), if $a$ is its scaled variable, and $b$ is its translated variable (like in Eq. (1)), as the change of the scale $a$, the corresponding maximum and minimum in continuous wavelet transform curve of original signal have a little difference. Along with the increase of the scale $a$, the local maximum and minimum points on the continuous wavelet transform curve become farther from the starting and ending points of saccade in HEO. So, according to the testing on training set, the scale $a$ was set to 8 for continuous wavelet transformation.

In Fig. 4, the black curve is the original signal containing saccade activities and the red curve is the continuous wavelet transformation of the original signal. The green stars in the red curve represent the maximums and the blue stars represent the minimums, and in the black curve the corresponding green stars and blue stars represent the starting points of saccade activities or the ending points of saccade activities. In Fig. 4, for a saccade activity $s_i$, which begins at the point $startS$ and ends with the point $endS$, and in the red curve if the corresponding maximum point of $startS$ is above the threshold and the the corresponding minimum point of $endS$ is below the minus threshold, this saccade activity $s_i$ is selected to form the whole saccade activities $S=[s_1, s_2...s_n]$. The corresponding length sequence for the $S$ is $L=[l_1,l_2...l_n]$.

We first calculated the difference of each saccade $s_i$ in $S$, then calculated the absolute value of the maximum of this difference as $m_i$ and the absolute value of the mean of this difference as $e_i$, so the corresponding vector $M=[m_1,m_2,...m_n]$ and $E=[e_1,e_2,...,e_n]$ are formed; The maximum in $M$ was defined as $M_f$, the mean of the $E$ was defined as $E_f$ and $P_f$ was defined as $E \ast L^T$; And the variance $V_f$ of the corresponding continuous wavelet transformation of this HEO is calculated. So, the features based on wavelet singularity analysis are:

$$F_1 = [M_f, E_f, P_f, V_f]$$  \hspace{1cm} (5)

If there are no green stars and blue stars outside the range $[\text{threshold}, -\text{threshold}]$ like in Fig. 5, then the values of corresponding features in Eq. (5) were all set to zero.

3) Features based on statistics: For each window data of 2s HEO, the following statistical features were extracted: a) The mean $A_1$, the variance $A_2$ and the entropy $A_3$ of the amplitude of signal. b) The mean $D_1$, the variance $D_2$ and the entropy $D_3$ of the difference of signal. c) The absolute value of the difference between the maximum and the minimum of the amplitude signal, denoted by $M_3$. Entropy is a thermodynamic quantity describing the amount of disorder in the system. It is used as a measure of the degree of order/disorder of signal, so it can provide useful information about the underlying dynamical process associated with the signal. In Fig. 6, the histogram of the signal amplitude and the entropy is calculated according to the amplitude probability distribution. The more uniform the distribution of the amplitude, the greater its entropy value. So the features based on statistics is:

$$F_2 = [A_1, A_2, A_3, D_1, D_2, D_3, M_3]$$  \hspace{1cm} (6)

The new features proposed in this study is defined as follows:

$$F_{DF} = [F_1, F_2]$$  \hspace{1cm} (7)

4) Features based on wavelet energy: Magosso et al. [3] used the wavelet energy to detect SEMs in sleep related research. These wavelet energy features also were used in our study to evaluate their performance. When frequency information is needed instead of the scales [14],

$$F_a = \frac{F_e}{\delta a}$$  \hspace{1cm} (8)
Therefore, wavelet energy feature vector can be expressed as:

\[ F_{WE} = [E_{P_{10}}, E_{D_{10}}, E_{D_{20}}, \ldots, E_{D_{10}}] \]

\[ E_{D_{j}} = \sum_{k} |C_{D_{j}}(k)|^2, j = 5, 6, \ldots, 10 \]

\[ E_{P_{10}} = \sum_{k} |C_{P_{10}}(k)|^2 \]

Therefore, wavelet energy feature vector can be expressed as:

\[ F_{WE} = [E_{P_{10}}, E_{D_{10}}, E_{D_{20}}, \ldots, E_{D_{10}}] \]

**B. Classifiers**

1) Support vector machine: Support vector machine is a classic and popular machine learning method for classification. The problem of training SVM is usually to solve its dual problem, and the decision function is:

\[ \text{sgn}(w^T \phi(x) + b) = \text{sgn}(\sum_{i=1}^{l} y_i a_i K(x_i, x) + b) \] (11)

Here, LIBSVM package was used and radial basis function (RBF) was selected. The range of the penalty factor \( C \) and the parameter \( \gamma \) of RBF were set to [0,1024] and [0,1,2], respectively. All of the points of \( (C, \gamma) \) were tried to find the best training result.

2) Graph regularized extreme learning machine: Graph regularized extreme Learning Machine (GELM) is based on the idea that similar samples should share similar properties and through adding a graph regularization term on the objective of conventional ELM to ensure the output of samples from the same class should be similar [13]. The standard ELM with \( K \) hidden nodes with activation function \( g(x) \) can be modeled as following:

\[ \sum_{j=1}^{K} \beta_j g(x_i) = \sum_{j=1}^{K} \beta_j (w_j \cdot x_i + b_j) = t_i, i = 1, \ldots, N \]

\[ x_i = (x_{i1}, x_{i2}, \ldots, x_{im})^T \text{ and } t_i = (t_{i1}, t_{i2}, \ldots, t_{im})^T \]

form the training data \( L = \{(x_i, t_i) | x_i \in \mathbb{R}^d, t_i \in \mathbb{R}^m\} \). The above \( N \) equations can be written as a matrix formulation as follows:

\[ H\beta = T \]

(13)

So the output weight of ELM can be determined by Eq. (14), in which \( H^T \) is the Moore-Penrose generalized inverse of \( H \).

\[ \beta^* = \arg \min_{\beta} \| H\beta - T \|_2^2 = H^T T \]

(14)

Suppose that \( y_i \) and \( y_j \) are the output vectors for \( h_i \) and \( h_j \) mapped by output weight matrix \( \beta \), \( h_i \) = \((g_1(x_i), \ldots, g_K(x_i))^T \) and \( h_j \) = \((g_1(x_j), \ldots, g_K(x_j))^T \).

The goal of GELM is to ensure that if two inputs \( x_i, x_j \) are from the same class, their outputs should be similar to each other. So we want to minimize the following objective function with the adjacent W:

\[ \min \sum_{i,j} ||y_i - y_j||^2 W_{ij} = Tr(YLY^T) \]

(15)

where \( Y = H\beta \), and adjacent W is defined as follows:

\[ W_{ij} = \begin{cases} 1/N_i, & \text{if both } h_i \text{ and } h_j \text{ belong to the } t \text{th class} \\ 0, & \text{otherwise} \end{cases} \]

(16)

By incorporating Eq. (15) and another regularization term into conventional ELM model, the objective function of GELM is:

\[ \min_{\beta} \| H\beta - T \|_2^2 + \lambda_1 Tr(H\beta L\beta^T H^T) + \lambda_2 \| \beta \|_2 \]

(17)
By setting the differentiate of above objective function with respect to $\beta$ as zero, we have
\[
\beta = (HH^T + \lambda_1HLH^T + \lambda_2I)^{-1}HT \quad (18)
\]
Eq. (18) makes the output weight matrix calculated directly.

### III. Material

#### A. Experiment

1) **Subjects:** Six normal students (4 male and 2 female, aged $22 \pm 3$) were recruited from Shanghai Jiao Tong University. Because the appearing of SEM was known to commonly occur in the beginning of sleep, and to ensure that the time epochs of SEM in every experiment were many enough, the students who had good regular sleeping habits were selected and the starting time of every experiment was one hour before their afternoon nap time about from 12:30 pm to 14:30 pm.

![Driving simulation environment](image)

**Fig. 7.** Driving simulation environment

2) **Procedure:** The driving simulator used in the experiment (Fig. 7), had a four-lane national highway with road signs and scenarios. Prior to the beginning of the experiment, the subject was required to do a ‘warm-up and training’ session lasting 10 min to be familiar with the vehicle controls. In this simulated scene, subjects as drivers were required to keep alertness all time as soon as possible and trying to suppress his/her sleepiness to avoid any traffic accidents. Each driving simulator experiment lasted for more than two hours.

3) **Data recording:** EOG were recorded by the NeuroScan system at a sampling rate 1000Hz, and a bandpass filtering between 0 and 40 Hz was done to remove irrelevant noise signals. The electrodes placement was the same as the conventional ones in EOG experiments analysis [3]. A camera was set to monitor the subject’s face to clearly recognize the opening or closing state of eyes. The subject’s face image from the camera and the real-time displaying of EOG signal in SCAN software were displayed at the same computer screen at the same time. And through the computer screen recording software, both together were recorded into the same video file. So with this video file, we could determine the eye state when SEM occurred. Because the waveform of VOR (Vestibuloocular reflex) is very similar to the SEM, so to avoid the error identification of SEM, subjects were instructed to keep their head motionless on the seat during the driving simulator experiment.

#### B. SEMs characteristics

SEMs are considered as reliable signs that sleep onset period has been entered, usually appear during the transition from wakefulness to sleep [2, 16]. According to our experiments, the following characteristics were verified:

1) **SEMs most occur with eyes closed:** Through looking back at the recorded video files, in which both the eye state (open or closed) and the EOG signal could be observed at the same moment, the conclusion of this check was that SEMs almost completely occurred when eyes closed and few occurred during the period of continuous frequent overlong blinks. Marzano *et.al.* mentioned that ‘slow ocular activity (SEM) could be a valid indicator of alertness only when eyes are closed and people are already falling asleep’ [16]. Even though SEM happened with eyes closed, but it is still useful in driving fatigue detection.

![SEM waveform](image)

**Fig. 8.** SEMs during a overlong eyelid closure when sleepy

When the driver is awake with eyes opening, fast eye movement and fixation are the main eye movements and there also exist more complicated eye movements which are caused by eye tracking the activities of objects.

2) **Relatively loose experiment restrictions:** Though the subjects were required to restrain drowsiness as far as possible, due to the simulated driving condition was much looser than real driving condition, the long time dozes with eyes closed
(most in the range of 4-10s, and few in 10-13s, and very few in 13-20s) were permissible and conducive to investigate the characteristics of EOG signals, because these long time epochs with eye closed (when SEM occurred) usually were not allowed to happen and would be big dangerous occurrences in real-world driving.

IV. Results

For bio-signal, individual variation usually exists, and the skin impedance value and the different skull structure will cause some signals’ amplitude differences in different subjects. Therefore, training and testing were done within the individual in this study.

In section III, we mentioned that the restriction of simulated driving experiments is relatively loose and allow the subjects to doze with some long times. But the whole time length of SEMs was still very shorter than the whole time length of non-SEMs, and the ratio between the two could be as high as 300:1 (non-SEMs:SEMs) (Table II). This is a problem of samples imbalance. To deal with imbalance problem, we use the two main schemes [7]: 1) Under-sampling the large class until it matches the size of the small class. 2) Over-sampling the small class until it contains as many samples as the other class.

Table II. The ratio between the SEMs and non-SEMs for six subjects’ sessions

<table>
<thead>
<tr>
<th>Session</th>
<th>SEMs(sec)</th>
<th>non-SEMs(sec)</th>
<th>Ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>451.4</td>
<td>6771</td>
<td>15:1</td>
</tr>
<tr>
<td>2</td>
<td>23.6</td>
<td>7209</td>
<td>305:1</td>
</tr>
<tr>
<td>3</td>
<td>182.7</td>
<td>7124</td>
<td>39:1</td>
</tr>
<tr>
<td>4</td>
<td>30.9</td>
<td>7201</td>
<td>233:1</td>
</tr>
<tr>
<td>5</td>
<td>449.4</td>
<td>7190</td>
<td>16:1</td>
</tr>
<tr>
<td>6</td>
<td>213.2</td>
<td>7038</td>
<td>33:1</td>
</tr>
</tbody>
</table>

For the under-sampling method, all SEM epochs and non-SEM epochs were divided into many 2s window data samples with a sliding step (s=0.3s). And after that if the number of SEMs with 2s time length was N, and the number of non-SEMs was M, so the first N/2 SEMs were put into training set. Because M was far larger than N, so the random selected N/2 non-SEMs were also put into training set. Then the rest N/2 SEMs and the random selected N/2 non-SEMs from the rest after the previous selection were put into testing set. Through this training and testing of 10 times, the mean performance of features was obtained by three classifiers respectively. To evaluate the performance of the features and classifiers, the following indicators were used to measure it.

Agreement=\(\frac{TP + TN}{\text{total number of samples}} \times 100\%\)

Sensitivity=\(\frac{TP}{TP + FN} \times 100\%\);

Selectivity=\(\frac{TP}{TP + FP} \times 100\%\);

where, \(TN\) is the number of negative samples correctly classified, \(FP\) is the number of negative samples incorrectly classified as positive, \(FN\) is the number of positive samples incorrectly classified as negative and \(TP\) is the number of positive samples correctly classified. In the following tables, WE represents wavelet energy features (\(F_{WE}\)), DF new defined features (\(F_{DF}\)) and BOTH means the combination of them. From Table III, we can find the overall performance of our new defined features is better than the only wavelet energy features, and by combination of this two features, the agreement value can be improved significantly. The next two tables (Table IV and Table V) give the corresponding sensitivity and the selectivity results of all subjects respectively. In general, the sensitivity results are a little sensitive to the kind of features and classifiers compared to the selectivity results.

Table III. The agreement of three classifiers over six subjects for the under-sampling method

<table>
<thead>
<tr>
<th>Feature Classifer</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
</tr>
</thead>
<tbody>
<tr>
<td>SVM</td>
<td>80.2</td>
<td>80.1</td>
<td>87.8</td>
<td>81.1</td>
<td>85.9</td>
<td>86.5</td>
</tr>
<tr>
<td>WE GELM</td>
<td>79.8</td>
<td>78.9</td>
<td>87.6</td>
<td>79.2</td>
<td>85.5</td>
<td>84.7</td>
</tr>
<tr>
<td>KNN</td>
<td>74.9</td>
<td>69.1</td>
<td>83.6</td>
<td>70.0</td>
<td>78.7</td>
<td>82.9</td>
</tr>
<tr>
<td>SVM</td>
<td>85.3</td>
<td>79.5</td>
<td>90.7</td>
<td>80.4</td>
<td>91.9</td>
<td>90.6</td>
</tr>
<tr>
<td>DF GELM</td>
<td>87.8</td>
<td>81.4</td>
<td>89.5</td>
<td>81.3</td>
<td>91.5</td>
<td>89.9</td>
</tr>
<tr>
<td>KNN</td>
<td>78.5</td>
<td>66.7</td>
<td>78.5</td>
<td>68.6</td>
<td>82.2</td>
<td>77.5</td>
</tr>
<tr>
<td>BOTH GELM</td>
<td>90.6</td>
<td>89.9</td>
<td>92.2</td>
<td>90.8</td>
<td>92.6</td>
<td>91.2</td>
</tr>
<tr>
<td>KNN</td>
<td>79.0</td>
<td>81.2</td>
<td>80.3</td>
<td>81.4</td>
<td>85.2</td>
<td>80.2</td>
</tr>
</tbody>
</table>

Table IV. The sensitivity results for the under-sampling method

<table>
<thead>
<tr>
<th>Feature Classifer</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
</tr>
</thead>
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<tr>
<td>SVM</td>
<td>76.2</td>
<td>82.3</td>
<td>91.4</td>
<td>83.3</td>
<td>86.5</td>
<td>90.9</td>
</tr>
<tr>
<td>WE GELM</td>
<td>74.4</td>
<td>82.9</td>
<td>90.1</td>
<td>83.9</td>
<td>88.2</td>
<td>90.8</td>
</tr>
<tr>
<td>KNN</td>
<td>61.5</td>
<td>52.1</td>
<td>77.3</td>
<td>57.1</td>
<td>72.2</td>
<td>78.6</td>
</tr>
<tr>
<td>SVM</td>
<td>89.5</td>
<td>78.5</td>
<td>93.9</td>
<td>75.5</td>
<td>92.7</td>
<td>92.8</td>
</tr>
<tr>
<td>DF GELM</td>
<td>89.8</td>
<td>78.8</td>
<td>95.3</td>
<td>76.1</td>
<td>92.7</td>
<td>93.6</td>
</tr>
<tr>
<td>KNN</td>
<td>67.2</td>
<td>50.1</td>
<td>69.5</td>
<td>58.5</td>
<td>73.1</td>
<td>72.8</td>
</tr>
<tr>
<td>SVM</td>
<td>91.3</td>
<td>80.2</td>
<td>96.8</td>
<td>82.8</td>
<td>92.3</td>
<td>97.0</td>
</tr>
<tr>
<td>BOTH GELM</td>
<td>91.8</td>
<td>82.6</td>
<td>96.7</td>
<td>84.5</td>
<td>92.5</td>
<td>97.1</td>
</tr>
<tr>
<td>KNN</td>
<td>71.9</td>
<td>60.2</td>
<td>71.6</td>
<td>62.2</td>
<td>78.23</td>
<td>70.9</td>
</tr>
</tbody>
</table>

Table V. The selectivity results for the under-sampling method

<table>
<thead>
<tr>
<th>Feature Classifer</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
</tr>
</thead>
<tbody>
<tr>
<td>SVM</td>
<td>82.9</td>
<td>79.8</td>
<td>85.4</td>
<td>79.2</td>
<td>85.7</td>
<td>86.3</td>
</tr>
<tr>
<td>WE GELM</td>
<td>83.5</td>
<td>76.8</td>
<td>81.8</td>
<td>78.2</td>
<td>84.2</td>
<td>82.8</td>
</tr>
<tr>
<td>KNN</td>
<td>83.9</td>
<td>78.7</td>
<td>86.6</td>
<td>76.1</td>
<td>83.3</td>
<td>88.6</td>
</tr>
<tr>
<td>SVM</td>
<td>82.9</td>
<td>88.2</td>
<td>88.3</td>
<td>88.1</td>
<td>91.4</td>
<td>89.2</td>
</tr>
<tr>
<td>DF GELM</td>
<td>83.4</td>
<td>85.1</td>
<td>85.2</td>
<td>86.4</td>
<td>91.8</td>
<td>91.1</td>
</tr>
<tr>
<td>KNN</td>
<td>83.2</td>
<td>77.5</td>
<td>85.0</td>
<td>78.5</td>
<td>89.6</td>
<td>86.9</td>
</tr>
<tr>
<td>SVM</td>
<td>88.8</td>
<td>90.0</td>
<td>88.7</td>
<td>90.0</td>
<td>93.0</td>
<td>88.7</td>
</tr>
<tr>
<td>BOTH GELM</td>
<td>88.6</td>
<td>86.5</td>
<td>86.2</td>
<td>87.3</td>
<td>92.8</td>
<td>86.2</td>
</tr>
<tr>
<td>KNN</td>
<td>89.7</td>
<td>83.6</td>
<td>87.0</td>
<td>83.6</td>
<td>91.2</td>
<td>85.0</td>
</tr>
</tbody>
</table>

For the over-sampling method, the sliding step \(s\) was used to over-sampling the class of SEMs until it contained as many samples as the non-SEMs. The operation for this was that if the ratio between the non-SEMs and SEMs was \(m:1\), then the sliding length of the sliding step was set to \(2s/m\), which was the window time length divided by \(m\). But the sliding step was only for the SEMs epochs not for non-SEMs epochs. Therefore, the number of SEMs was almost equal to the number of non-SEMs, and half of them respectively were put into training set and the rest of them into testing set. In the
Table VI we can see, by over-sampling the SEMs epoches, the agreements of all subjects could become very high, compared to the under-sampling method. The reason for this results may be, on the one hand, to reach this size of non-SEMs the number of training samples was dramatically expanded, and on the other hand, by the very tiny time length of sliding step (such as 2s/305.5 = 0.0065s), more similar SEMs were generated and thus easy to recognize. Another reason might be partly that the database was simple and small.

However, for the VOR, which is SEM-like eye movement, the algorithm still can not distinguish and the experiments limited the generation of VOR in order to determine the eye closed state when SEM occurred.

V. CONCLUSIONS

The occurrence of slow eye movement means that the driver is about to enter the initial stage of sleep, so it is extremely dangerous and in urgent need of detecting it. This study discusses the characteristics of slow eye movement in the driving simulation experiments and proposed new features based on wavelet singularity analysis and statistics to improve the detection effect of SEMs. Experiments results indicate new defined features are a little better than the wavelet energy, and the combination of wavelet energy features and new defined features are a little better than the wavelet energy, and the combination of wavelet energy features and new defined features can obtain better classification results than each single kind of features. In the real-world driving environment, there are more complicated eye movements such as VOR and smooth pursuit, which will bring difficulties for detecting SEMs. Therefore, that will be further studied for SEM recognition in our future work.

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