

# Fourth-Order Dependency Parsing\*

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## ABSTRACT

We present and implement a fourth-order projective dependency parsing algorithm that effectively utilizes both “grand-sibling” style and “tri-sibling” style interactions of third-order and “grand-tri-sibling” style interactions of fourth-order factored parts for performance enhancement. This algorithm requires  $O(n^5)$  time and  $O(n^4)$  space. We implement and evaluate the parser on two languages—English and Chinese, both achieving state-of-the-art accuracy. This results show that a higher-order ( $\geq 4$ ) dependency parser gives performance improvement over all previous lower-order parsers.

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KEYWORDS: Dependency Parsing, Fourth-order.

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## 1 Introduction

In recent years, dependency parsing has gained universal interest due to its usefulness in a wide range of applications such as synonym generation (Shinyama et al., 2002), relation extraction (Nguyen et al., 2009) and machine translation (Katz-Brown et al., 2011; Xie et al., 2011).

CoNLL-X shared task on dependency parsing (Buchholz and Marsi, 2006; Nivre et al., 2007) made a comparison of many algorithms, and graph-based parsing models have achieved state-of-the-art accuracy for a wide range of languages. Graph-based dependency parsing algorithms usually use the factored representations of dependency trees: a set of small *parts* with special structures. The types of features that the model can exploit depend on the information included in the factorizations. Several previous works have shown that higher-order parsers utilizing richer contextual information achieve higher accuracy than lower-order ones—Chen et al. (2010) illustrated that a wide range of decision history can lead to significant improvements in accuracy for graph-based dependency parsing models. Meanwhile, several previous works (Carreras, 2007; Koo and Collins, 2010) have shown that grandchild interactions provide important information for dependency parsing. However, the computational cost of the parsing algorithm increases with the need for more expressive factorizations. Consequently, the existing most powerful parser (Koo and Collins, 2010) is limited to third-order parts, which requires  $O(n^4)$  time and  $O(n^3)$  space.

In this paper, we further present a fourth-order parsing algorithm that can utilize more richer information by enclosing grand-sibling and tri-sibling parts into a grand-tri-sibling part. Koo and Collins (2010) discussed the possibility that the third-order parsers are extended to fourth-order by increasing vertical context (e.g. from grand-siblings to “great-grand-siblings”) or horizontal context (e.g. from grand-siblings to “grand-tri-siblings”), and Koo (2010) first described this algorithm. In this work, we show that grand-tri-siblings can effectively work. The computational requirements of this algorithm are  $O(n^3)$  time and  $O(n^4)$  space. To achieve empirical evaluations of our parser, we implement and evaluate the proposed parsing algorithm on the Penn WSJ Treebank (Marcus et al., 1993) for English, and Penn Chinese Treebank (Xue et al., 2005) for Chinese, both achieving state-of-the-art accuracy. A free distribution of our implementation in C++ has been put on the Internet.<sup>1</sup>

## 2 Related Work

There have been several existing graph-based dependency parsing algorithms, which are the backbones of the new fourth-order dependency parser. In this section, we mainly describe four graph-based dependency parsers with different types of factorization.

The first-order parser (McDonald et al., 2005) decomposes a dependency tree into its individual edges. Eisner (2000) introduced a widely-used dynamic programming algorithm for first-order parsing, which is to parse the left and right dependents of a word independently, and combine them at a later stage. This algorithm introduces two types of dynamic programming structures: *complete* spans, and *incomplete* spans (McDonald, 2006). Larger spans are created from two smaller, adjacent spans by recursive combination in a bottom-up procedure.

McDonald and Pereira (2006) defined a second-order sibling dependency parser in which interactions between adjacent siblings are allowed. Koo and Collins (2010) proposed an algorithm

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<sup>1</sup><http://sourceforge.net/projects/maxparser/>

that factors each dependency tree into a set of *grandchild* parts. Formally, a grandchild part is a triple of indices  $(g, s, t)$  where  $g$  is the head of  $s$  and  $s$  is the head of  $t$ . In order to parse this factorization, it is necessary to augment both complete and incomplete spans with grandparent indices. Following Koo and Collins (2010), we refer to these augmented structures as *g-spans*. The second-order parser proposed in Carreras (2007) is capable of scoring both sibling and grandchild parts with complexities of  $O(n^4)$  time and  $O(n^3)$  space. However, the parser suffers a crucial limitation that it can only evaluate events of grandchild parts for outermost grandchildren.

Koo and Collins (2010) proposed a third-order grand-sibling parser that decomposes each tree into set of *grand-sibling* parts—parts combined with sibling parts and grandchild parts. This factorization defines all grandchild and sibling parts and still requires  $O(n^4)$  time and  $O(n^3)$  space. Koo and Collins (2010) also discussed the possibility that the third-order parsers are extended to fourth-order by increasing vertical context or horizontal context and Koo (2010) first described this algorithm.

Zhang and McDonald (2012) generalized the Eisner (1996) algorithm to handle arbitrary features over higher-order dependencies. However, their generalizing algorithm suffers quite high complexities of time and space – for instance, the parsing complexity of time is  $O(n^5)$  for a third-order factored model. In order to achieve asymptotic efficiency of cost, cube pruning for decoding is utilized (Chiang, 2007).

Another dominant category of data-driven dependency parsing systems is local-and-greedy transition-based parsing (Yamada and Matsumoto, 2003; Nivre and Scholz, 2004; Attardi, 2006; McDonald and Nivre, 2007) which parameterizes models over transitions from state to another in an abstract state-machine. In these models, dependency trees are constructed by making a series of incremental decisions. Parameters in these models are typically learned using standard classification techniques.

### 3 Fourth-Order Parsing Algorithm

In this section, we propose our fourth-order dependency parsing algorithm, which factors each dependency tree into a set of *grand-tri-sibling* parts. Specifically, a grand-tri-sibling is a 5-tuple of indices  $(g, s, r, m, t)$  where  $(s, r, m, t)$  is a tri-sibling part and  $(g, s, r, m)$  and  $(g, s, m, t)$  are grand-sibling parts.

The algorithm is characterized by introducing a new type incomplete g-spans structure: grand-sibling-spans or *gs-spans*, by augmenting incomplete g-spans with a sibling index. Formally, we denote gs-spans as  $[g, s, m, t]$  where  $[g, s, t]$  is a normal incomplete g-span and  $m$  is an index lying in the strict interior of the range  $[s, t]$ , such that  $(s, m, t)$  forms a valid sibling part.

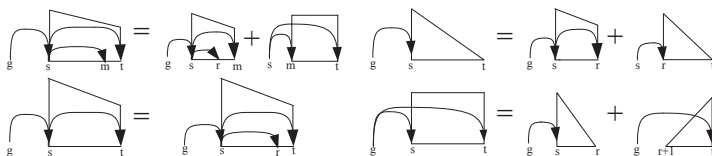


Figure 1: The dynamic-programming structures and derivation of fourth-order grand-tri-sibling parser. Symmetric right-headed versions are elided for brevity.

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Initialization:  $C[g][s][s][d][c] = 0.0 \quad \forall g, s, d, c$ 
for  $k : 1..n$ 
  for  $s : 0..n - k$ 
    for  $t = s + k$ 
      for  $g < s$  or  $g > t$ 
        for  $m > s$  and  $m < t$ 
           $D[g][s][m][t][\rightarrow] = C[s][s+1][m][\leftarrow][1] + S(g, s, -, -, m) + C[s][m][t][-][2] + S(g, s, -, m, t)$ 
           $D[g][s][m][t][\leftarrow] = C[t][m][t-1][\rightarrow][1] + S(g, t, -, -, m) + C[t][s][m][-][2] + S(g, t, -, m, s)$ 

           $D[g][s][m][t][\rightarrow] = \max\{D[g][s][m][t][\leftarrow], \max_{s < r < m} \{D[g][s][r][m][\rightarrow] + C[s][m][t][-][2] + S(g, s, r, m, t)\}\}$ 
           $D[g][s][m][t][\leftarrow] = \max\{D[g][s][m][t][\rightarrow], \max_{m < r < t} \{D[g][m][r][t][\leftarrow] + C[t][s][m][-][2] + S(g, t, r, m, s)\}\}$ 
        end for
         $C[g][s][t][-][2] = \max_{s \leq r < t} \{C[g][s][r][\rightarrow][1] + C[g][r+1][t][\leftarrow][1]\}$ 

         $C[g][s][t][\rightarrow][0] = C[g][s][s][\leftarrow][1] + C[s][s+1][t][\leftarrow][1] + S(g, s, -, -, t)$ 
         $C[g][s][t][\leftarrow][0] = C[g][t][t][\rightarrow][1] + C[t][s][t-1][\rightarrow][1] + S(g, t, -, -, s)$ 

         $C[g][s][t][\rightarrow][0] = \max\{C[g][s][t][\rightarrow][0], \max_{s < r < t} \{D[g][s][r][t][\rightarrow]\}\}$ 
         $C[g][s][t][\leftarrow][0] = \max\{C[g][s][t][\leftarrow][0], \max_{s < r < t} \{D[g][s][r][t][\leftarrow]\}\}$ 

         $C[g][s][t][\rightarrow][1] = \max_{s < r \leq t} \{C[g][s][r][\rightarrow][0] + C[s][r][t][\rightarrow][1]\}$ 
         $C[g][s][t][\leftarrow][1] = \max_{s \leq r < t} \{C[g][r][t][\leftarrow][0] + C[t][s][r][\leftarrow][1]\}$ 
      end for
    end for
  end for
end for

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Figure 2: Pseudo-code of bottom-up chart parser for fourth-order grand-tri-sibling parsing algorithm

Figure 1 provides a graphical specification of the fourth-order grand-tri-sibling parsing algorithm. An incomplete gs-span is constructed by combining a smaller incomplete gs-span, representing the next-innermost pair of modifiers, with a sibling gs-span. The algorithm resembles the third-order grand-sibling parser except that the incomplete g-spans are constructed by an incomplete gs-span with the same region.

We will now describe the fourth-order grand-tri-sibling parsing algorithm in more detail. Like factored parsing algorithms presented in the previous section, this parsing algorithm can be parsed via adaptations of standard chart-parsing techniques. Following McDonald (2006), let  $C[g][s][t][d][c]$  be a dynamic programming table that stores the score of the best subtree from position  $s$  to position  $t$ ,  $s < t$ , with grandparent position  $g$ , direction  $d$  and complete value  $c$ . The variable  $d \in \{\leftarrow, \rightarrow\}$  indicates the direction of the subtree (gathering left or right dependents). The variable  $c \in \{0, 1, 2\}$  indicates if a subtree is complete ( $c = 1$ ), incomplete ( $c = 0$ ) or represents sibling subtrees ( $c = 2$ ). Sibling types have no inherent direction, so it will be always able to assume that when  $c = 2$  then  $d = null(-)$ . We introduce another dynamic programming table  $D[g][s][m][t][d]$  to store the score of the best gs-span from position  $s$  to position  $t$ ,  $s < t$ , with grandparent position  $g$ , sibling position  $m$  and direction  $d$ . Since gs-spans are all incomplete ( $c = 1$ ), the complete value can be omitted. Pseudo code for filling up the dynamic programming tables is in Figure 2. Since the introduction of gs-span, this parsing algorithm requires  $O(n^5)$  time and  $O(n^4)$  space.

grand-sibling features for part ( $g, s, m, t$ )			
<b>4-gram features</b>		<b>context features</b>	
L(g)·P(s)·P(m)·P(t)		P(g)·P(s)·P(m)·P(t)·P(g+1)·P(s+1)·P(t+1)	
P(g)·L(s)·P(m)·P(t)		P(g)·P(s)·P(m)·P(t)·P(g-1)·P(s-1)·P(t-1)	
P(g)·P(s)·L(m)·P(t)		P(g)·P(s)·P(m)·P(t)·P(g+1)·P(s+1)	
P(g)·P(s)·P(m)·L(t)		P(g)·P(s)·P(m)·P(t)·P(g-1)·P(s-1)	
L(g)·L(s)·P(m)·P(t)		P(g)·P(m)·P(t)·P(g+1)·P(m+1)·P(t+1)	
L(g)·P(s)·L(m)·P(t)		P(g)·P(m)·P(t)·P(g+1)·P(m-1)·P(t-1)	
L(g)·P(s)·P(m)·L(t)		P(g)·P(m)·P(g+1)·P(m+1)	
P(g)·L(s)·L(m)·P(t)		P(g)·P(m)·P(g-1)·P(m-1)	
L(g)·L(s)·P(m)·L(t)		P(g)·P(t)·P(g+1)·P(t+1)	
P(g)·P(s)·L(m)·L(t)		P(g)·P(t)·P(g-1)·P(t-1)	
P(g)·P(s)·P(m)·P(t)		P(m)·P(t)·P(m+1)·P(t+1)	
		P(m)·P(t)·P(m-1)·P(t-1)	
<b>coordination features</b>		<b>backed-off features</b>	
L(g)·L(s)·L(t)	L(g)·P(s)	P(s)·P(t)	L(g)·P(m)·P(t)
L(g)·P(s)·P(t)	P(g)·L(s)	P(g)·P(s)	L(g)·P(m)·L(t)
P(g)·L(s)·P(t)	L(g)·P(t)	P(g)·L(t)	P(g)·P(m)·L(t)
P(g)·P(s)·L(t)	P(g)·P(t)	L(s)·P(t)	P(g)·P(m)·P(t)
L(g)·L(s)·P(t)	P(g)·P(s)·P(t)	P(s)·L(t)	L(g)·L(m)·P(t)
L(g)·P(s)·L(t)	P(g)·L(s)·L(t)		
tri-sibling features for part ( $s, r, m, t$ )			
<b>4-gram features</b>		<b>backed-off features</b>	
L(s)·P(r)·P(m)·P(t)	L(s)·P(r)·P(m)·L(t)	L(r)·P(m)·P(t)	P(r)·P(m)·P(t)
P(s)·L(r)·P(m)·P(t)	P(s)·L(r)·L(m)·P(t)	P(r)·L(m)·P(t)	L(r)·L(t)
P(s)·P(r)·L(m)·P(t)	P(s)·L(r)·P(m)·L(t)	P(r)·P(m)·L(t)	L(r)·P(t)
P(s)·P(r)·P(m)·L(t)	P(s)·P(r)·L(m)·L(t)	L(r)·L(m)·P(t)	P(r)·L(t)
L(s)·L(r)·P(m)·P(t)	P(s)·P(r)·P(m)·P(t)	L(r)·P(m)·L(t)	P(r)·P(t)
L(s)·P(r)·L(m)·P(t)		P(r)·L(m)·L(t)	
<b>context features</b>			
P(r)·P(m)·P(t)·P(r+1)·P(m+1)·P(t+1)		P(r)·P(m)·P(r+1)·P(m+1)	
P(r)·P(m)·P(t)·P(r-1)·P(m-1)·P(t-1)		P(r)·P(m)·P(r-1)·P(m-1)	
P(s)·P(r)·P(m)·P(t)·P(s+1)·P(r+1)		P(r)·P(t)·P(r+1)·P(t+1)	
P(s)·P(r)·P(m)·P(t)·P(s-1)·P(r-1)		P(r)·P(t)·P(r-1)·P(t-1)	
P(s)·P(r)·P(m)·P(t)·P(r+1)·P(t+1)		P(m)·P(t)·P(m+1)·P(t+1)	
P(s)·P(r)·P(m)·P(t)·P(r-1)·P(t-1)		P(m)·P(t)·P(m-1)·P(t-1)	
P(s)·P(r)·P(m)·P(t)·P(s+1)·P(r+1)·P(t+1)		P(s)·P(r)·P(m)·P(t)·P(s+1)·P(t+1)	
P(s)·P(r)·P(m)·P(t)·P(s-1)·P(r-1)·P(t-1)		P(s)·P(r)·P(m)·P(t)·P(s-1)·P(t-1)	
grand-tri-sibling features for part ( $g, s, r, m, t$ )			
<b>5-gram features</b>		<b>4-gram backed-off features</b>	
L(g)·P(s)·P(r)·P(m)·P(t)	P(g)·L(s)·P(r)·P(m)·P(t)	L(g)·P(r)·P(m)·P(t)	P(g)·L(r)·P(m)·P(t)
P(g)·P(s)·L(r)·P(m)·P(t)	P(g)·P(s)·P(r)·L(m)·P(t)	P(g)·P(r)·L(m)·P(t)	P(g)·P(r)·P(m)·L(t)
P(g)·P(s)·P(r)·P(m)·L(t)	P(g)·P(s)·P(r)·P(m)·P(t)	P(g)·P(r)·P(m)·P(t)	

Table 1: All feature templates used by the fourth-order grand-tri-sibling parser. L(·) and P(·) are the lexicon and POS tag of each token.

## 4 Feature Space

Following previous works (McDonald and Pereira, 2006; Koo and Collins, 2010), the fourth-order parser captures not only features associated with corresponding fourth-order grand-tri-sibling parts, but also the features of relevant lower-order parts that are enclosed in its factorization.

The lower-order features (first-order features of dependency parts and second-order features of grandchild and sibling parts) are based on feature sets from previous work (McDonald et al., 2005; McDonald and Pereira, 2006; Carreras, 2007). We added lexicalized versions of several features. For example, second-order grandchild feature set defines lexical trigram features, while previous work only used POS trigram features.

Table 1 outlines all feature templates of third-order grand-sibling, third-order tri-sibling, and fourth-order grand-tri-sibling parts. The fourth-order feature set consists of two sets of features. The first set of features is defined to be *5-gram features* that is a 5-tuple consisting of five relevant indices using words and POS tags. The second set of features is defined as *backed-off features* (Koo and Collins, 2010) for grand-tri-sibling part  $(g, s, r, m, t)$ —the 4-gram  $(g, r, m, t)$ , which never exist in any lower-order part. The determination of this feature set is based on experiments on the development data for both English and Chinese. In section 5.1 we examine the impact of these new features on parsing performance.

According to Table 1, several features in our parser depend on part-of-speech (POS) tags of input sentences. For English, POS tags are automatically assigned by the SVMTool tagger (Gimenez and Marquez, 2004). The accuracy of the SVMTool tagger on PTB is 97.3%; For Chinese, we used gold-standard POS tags in CTB. Following Koo and Collins (2010), two versions of POS tags are used for any features involve POS: one using is normal POS tags and another is a coarsened version of the POS tags.<sup>2</sup>

## 5 Experiments

The proposed fourth-order dependency parsing algorithm is evaluated on the Penn English Treebank (PTB 3.0) (Marcus et al., 1993) and the Penn Chinese Treebank (CTB 5.0).

For English, the PTB data is prepared by using the standard split: sections 2-21 are used for training, section 22 is for development, and section 23 for test. For Chinese, we adopt the identical training/validation/testing data split and experimental set-up as Zhang and Clark (2009). Dependencies are extracted by using Penn2Malt<sup>3</sup> tool.

Parsing accuracy is measured with unlabeled attachment score (UAS): the percentage of words with the correct head, and the percentage of complete matches (CM).<sup>4</sup>

The  $k$ -best version of the Margin Infused Relaxed Algorithm (MIRA) (Crammer and Singer, 2003; Crammer et al., 2006; McDonald, 2006) for the max-margin models (Taskar et al., 2003) is chosen for parameter estimation of our parsing model. In practice, we set  $k = 10$  and exclude the sentences containing more than 100 words in both the training data sets of English and Chinese in all experiments.<sup>5</sup>

<sup>2</sup>For English, we used first two characters of the tag, except PRP\$; For Chinese, we dropped the last character, except PU and CD

<sup>3</sup><http://w3.msi.vxu.se/~nivre/research/Penn2Malt.html>

<sup>4</sup>As in previous work, English evaluation ignores any token whose gold-standard POS tag is one of { " " : , , . }, and Chinese evaluation ignores any token whose tag is "PU".

<sup>5</sup>The number of sentences with more than 100 words is 3 for PTB and 67 for CTB.

Feature	Eng		Chn	
	UAS	CM	UAS	CM
baseline	93.45	49.06	87.38	38.85
+tri-sibling	93.62	49.42	87.60	38.94
+grand-tri-sibling	93.70	49.76	87.69	39.12
+4-gram backed-off	93.77	50.82	87.74	39.23

Table 2: The effect of different types of features on the development sets for English and Chinese.

## 5.1 Development Experiments

In this section, we dissect the contributions of each type of features. Table 2 shows the effect of different types of features on the development data sets for English and Chinese. Each row in Table 2 uses a super set of features than the previous one. Third-order grand-sibling parser is used as the baseline, and third-order tri-sibling, 5-gram grand-tri-sibling and 4-gram backed-off feature templates in Table 1 are incrementally added. All systems use our proposed fourth-order parsing algorithm. Since the only difference between systems is the set of features used, we can analyze the improvement from additional features.

From Table 2, we can see that each of the following parser capturing a group of new feature templates makes improvement on parsing performance over the previous one. Thus, we can conclude that the improvements come from the factorization’s ability of capturing richer features which contains more context information. The parser with all these features achieves UAS of 93.77% and CM of 50.82% on PTB and UAS of 87.74%, CM of 39.23% on CTB.

## 5.2 Results and Analysis

Our parser obtains UAS of 93.4% and CM 50.3% of on PTB, and UAS of 87.4%, CM of 36.8% on CTB. Both of the results are state-of-the-art performance on these two treebanks.

Table 3 illustrates the UAS and CM of the fourth-order parser on PTB, together with some relevant results from related work. We compare our method to first-order and second-order sibling dependency parsers (McDonald and Pereira, 2006), and two third-order graph-based parsers (Koo and Collins, 2010). Additionally, we compare to a state-of-the-art graph-based parser (Zhang and McDonald, 2012) as well as a state-of-the-art transition-based parser (Zhang and Nivre, 2011).

Our experimental results show an improvement in performance over the results in Zhang and Nivre (2011), which are based on a transition-based dependency parser with rich non-local features. Our results are also better than the results of the two third-order graph-based dependency parsing models in Koo and Collins (2010). Moreover, our algorithm achieves better parsing performance than the generalized higher-order parser with cube-pruning (Zhang and McDonald, 2012), which is the state-of-the-art graph-based dependency parser so far. The models marked † or ‡ are not directly comparable to our work. The models marked † use semi-supervised methods with large amount of unlabeled data, and those marked ‡ utilize phrase-structure annotations, while our parser obtains results competitive with these works. All three models marked † or ‡ are based on the Carreras (2007) parser, which might be replaced by our fourth-order parser to get an even better performance.

Parser	UAS	CM
McDonald and Pereira (2006), 1 <sup>st</sup> order	90.9	36.7
McDonald and Pereira (2006), 2 <sup>nd</sup> order	91.5	42.1
Zhang and Clark (2008)	92.1	45.4
Zhang and Nivre (2011)	92.9	48.0
Koo and Collins (2010), model 2	92.9	–
Koo and Collins (2010), model 1	93.0	–
Zhang and McDonald (2012)	93.1	–
<b>this paper</b>	<b>93.4</b>	<b>50.3</b>
Koo et al. (2008) <sup>†</sup>	93.2	–
Carreras et al. (2008) <sup>‡</sup>	93.5	–
Suzuki et al. (2009) <sup>†</sup>	93.8	–

Table 3: UAS and CM of different parsers on PTB 3.0

Parser	UAS	CM
Huang and Sagae (2010)	85.2	33.7
Zhang and Clark (2008)	85.7	34.4
Zhang and Nivre (2011)	86.0	36.9
3 <sup>rd</sup> order grand-sibling	86.8	35.5
Zhang and McDonald (2012)	86.9	–
<b>this paper</b>	<b>87.4</b>	<b>36.8</b>
Zhang and Clark (2009) <sup>‡</sup>	86.6	36.1

Table 4: UAS and CM of different parsers on CTB 5.0

Next, we turn to the impact of our fourth-order parser on Chinese. Table 4 shows the comparative results for Chinese. Here we compare our method to an implement of the third-order grand-sibling parser — whose parsing performance on CTB is not reported in Koo and Collins (2010), and the dynamic programming transition-based parser of Huang and Sagae (2010). Additionally, we compare to the state-of-the-art graph-based dependency parser (Zhang and McDonald, 2012) as well as a state-of-the-art transition-based parser (Zhang and Nivre, 2011). The results indicates that our parser achieved significant improvement of the previous systems on this data set. The parsing model of Zhang and Clark (2009), which is marked ‡, also depends on phrase-structure annotations. So it cannot compare with ours directly, even through our results are better.

## 6 Conclusion

We have presented an even higher-order projective dependency parsing algorithm that can evaluate the fourth-order sub-structures of grand-tri-siblings. This algorithm achieves stage-of-the-art performance on both PTB and CTB, which demonstrates that the fourth-order grand-tri-sibling features have important contribution to dependency parsing.

A wide range of further research involving the fourth-order parsing algorithm is available. One idea would be to identify the highest  $n$  for which the information of  $n$ th-order part still improves parsing performance. Moreover, as the fourth-order parser has achieved state-of-the-art accuracy on standard parsing benchmarks, many NLP tasks may benefit from it.



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